

| COURSE INFORMATION | | | | | |
|-----------------------------|-----------------|----------|--------------|----------|-----------|
| Course Title | Code | Semester | L+P Hour | Credits | ECTS |
| STOCHASTIC PROCESSES | ESYE 540 | 1 | 3 + 0 | 3 | 10 |

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| Prerequisites | |
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| Language of Instruction | English |
| Course Level | Master's Degree |
| Course Type | Elective |
| Course Coordinator | |
| Instructors | |
| Assistants | |
| Goals | This course aims to help students acquire both the mathematical principles and the intuition necessary to create, analyze, and understand insightful models for a broad range of various stochastic processes. |
| Content | A short review of the concepts of probability which is followed by the basic theory of the Laws of Large numbers and Bernoulli Processes. The course then includes Poisson process, Renewal processes, Markov chains in discrete and continuous time, as well as Brownian motion and Random walks. Applications of these stochastic processes are emphasized by examples. |

| Course Learning Outcomes | Program Learning Outcomes | Teaching Methods | Assessment Methods |
|---|---------------------------|------------------|--------------------|
| 1) Proficient in fundamental probability concepts | 1,2,4 | 1,2,4 | A, C |
| 2) Experienced in basic theory of probability | 1,2,4 | 1,2,4 | A, C |
| 3) Achieves probabilistic intuition and insight in thinking about problems | 1,2,4 | 1,2,4 | A, C |
| 4) Attains a moderate and practical knowledge in both Discrete and Continuous Markov Chains | 1,2,4 | 1,2,4 | A, C |
| 5) Uses theoretically studied methods on queuing systems and uses models to determine whether systems are reliable. | 1,2,4 | 1,2,4 | A, C |

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|---|-------|-------|------|
| 6) Becomes familiar with the application of stochastic processes in fields such as engineering, management sciences and operational research. | 1,2,4 | 1,2,4 | A, C |
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| Teaching Methods: | 1: Lecture, 2: Question-Answer, 3: Lab, 4: Case-study |
| Assessment Methods: | A: Testing, B: Experiment, C: Homework, D: Project |

| COURSE CONTENT | | |
|-----------------------|--|------------------------------------|
| Week | Topics | Study Materials |
| 1 | INTRODUCTION AND REVIEW OF PROBABILITY | Textbook, Course Notes |
| 2 | BERNOULLI PROCESSES | Textbook, Course Notes |
| 3 | LAWS OF LARGE NUMBERS, CONVERGENCE | Textbook, Course Notes |
| 4 | POISSON PROCESSES | Textbook, Course Notes |
| 5 | RENEWAL THEORY | Textbook, Course Notes, Case study |
| 6 | RENEWAL REWARD PROCESSES | Textbook, Course Notes, Case study |
| 7 | MARKOV CHAINS | Textbook, Course Notes, Case study |
| 8 | MIDTERM EXAM | Textbook, Course Notes |
| 9 | CONTINUOUS TIME MARKOV CHAINS | Textbook, Course Notes |
| 10 | BIRTH AND DEATH PROCESSES | Textbook, Course Notes |
| 11 | QUEUEING THEORY | Textbook, Course Notes, Case study |
| 12 | RELIABILITY THEORY | Textbook, Course Notes, Case study |
| 13 | RANDOM WALKS | Textbook, Course Notes |
| 14 | BROWNIAN MOTION AND STATIONARY PROCESSES | Textbook, Course Notes, Case study |

| RECOMMENDED SOURCES | |
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| Textbook | INTRODUCTION TO PROBABILITY MODELS 10TH EDITION, SHELDON M. ROSS, ELSEVIER, 2010 |
| Additional Resources | STOCHASTIC PROCESSES 2ND EDITION, SHELDON M. ROSS, WILEY 1996 |

| MATERIAL SHARING | |
|-------------------------|------------------------------------|
| Documents | Modeling case study, lecture notes |
| Assignments | Homeworks 1-6 |
| Exams | Midterm 1, Final Exam |

| ASSESSMENT | | | |
|---|------------------------|---------------|-------------------|
| | IN-TERM STUDIES | NUMBER | PERCENTAGE |
| Midterm 1 | | 1 | 45 |
| Homeworks | | 6 | 55 |
| | Total | | 100 |
| CONTRIBUTION OF FINAL EXAMINATION TO OVERALL GRADE | | | 30 |
| CONTRIBUTION OF IN-TERM STUDIES TO OVERALL GRADE | | | 70 |
| | Total | | 100 |

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|------------------------|-------------------------|
| COURSE CATEGORY | Expertise/Field Courses |
|------------------------|-------------------------|

| COURSE'S CONTRIBUTION TO PROGRAM | | | | | | |
|---|--|--------------|---|----------|---|----------|
| No | Program Learning Outcomes | Contribution | | | | |
| | | 1 | 2 | 3 | 4 | 5 |
| 1 | Adequate background in Mathematics, Natural Sciences and the Industrial and Systems Engineering discipline. | | | | | X |
| 2 | Ability to identify, model and solve complex problems in the area of Industrial and Systems Engineering. | | | | | X |
| 3 | Ability to design a complex system, process, device or product under realistic constraints and conditions, in such a way as to meet the desired requirements. | | | X | | |
| 4 | Ability to employ information technologies effectively in Industrial and Systems Engineering applications and develop and/or use modern techniques and tools for these applications. | | | X | | |

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| 5 | Ability to design and conduct experiments and interpret results to analyze problems in the area of Industrial and Systems Engineering. | | | | | X | |
| 6 | Ability to take responsibility both individually and as a team member to solve unforeseen problems that arise in intra-disciplinary and inter-disciplinary projects. | | | | | | |
| 7 | Ability to access information in the area of Industrial and Systems Engineering and to report and communicate this information to others using a foreign language (English) at the European Language Portfolio C1 General Level. | | | | | | |
| 8 | Ability to follow current issues and recent developments in science and technology by accessing databases and other sources of information and to continue to educate oneself. | | | | | | |
| 9 | Awareness of scientific and ethical responsibility in professional matters. | | | | | | |
| 10 | Ability to initiate innovative projects in the area of Industrial and Systems Engineering and to manage these projects considering all aspects. | | | | | | |
| 11 | Ability to identify the impact of Industrial and Systems Engineering applications on health, environment and safety; awareness of the legal consequences of Industrial and Systems Engineering solutions. | | | | | | |

ECTS ALLOCATED BASED ON STUDENT WORKLOAD BY THE COURSE DESCRIPTION

| Activities | Quantity | Duration (Hour) | Total Workload (Hour) |
|--|----------|-----------------|-----------------------|
| Course Duration (Excluding the exam weeks: 12x Total course hours) | 12 | 3 | 36 |
| Hours for off-the-classroom study (Pre-study, practice) | 14 | 10 | 140 |
| Midterm examination | 1 | 3 | 3 |
| Homework | 6 | 10 | 60 |
| Final examination | 1 | 3 | 3 |
| Total Work Load | | | 242 |
| Total Work Load / 25 (h) | | | 9.68 |
| ECTS Credit of the Course | | | 10 |